

Grade IX
Mathematics – Chapter I

1. Find the decimal expansion of $\frac{10}{3}$, $\frac{7}{8}$, and $\frac{1}{7}$

$3.333 \dots$ $\begin{array}{r} 3 \overline{) 10} \\ \underline{9} \\ 10 \\ \underline{9} \\ 10 \\ \underline{9} \\ 10 \\ \underline{9} \\ 1 \end{array}$	0.875 $\begin{array}{r} 8 \overline{) 7.0} \\ \underline{64} \\ 60 \\ \underline{56} \\ 40 \\ \underline{40} \\ 00 \end{array}$	$0.142857 \dots$ $\begin{array}{r} 10 \\ \underline{7} \\ 30 \\ \underline{28} \\ 20 \\ \underline{14} \\ 60 \\ \underline{56} \\ 40 \\ \underline{35} \\ 50 \\ \underline{49} \\ 1 \end{array}$
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$$\frac{10}{3}$$

Solution: (i) Quotient; 3.333...

(ii) Divisor: 3

(iii) Remainder = 1

2. Express 3.142678 as a rational number.

$$\text{Solution: } 3.142678 = \frac{3142678}{1000000}$$

3. Show that $0.3333 \dots = 0.\bar{3}$ (Read block at 3) can be expressed in the form of $\frac{p}{q}$.

Where p and q are integers and $q \neq 0$.

Solution\; Since we donot know what $0.\bar{3}$ is, let's ca;; it x and $80 \times x = 0.3333 \dots$

$$10x = 3.333 \dots$$

$$3.3333 \dots = 3 + x \text{ [because } x = 0.3333 \dots]$$

$$\therefore 10x = 3 + x$$

$$10x - x = 3$$

$$9x = 3 \therefore x = \frac{3}{9} = \frac{1}{3} = 0.3333 \dots = 0.\bar{3}$$

4. Show that $1.272727 \dots = 1.\bar{27}$ can be expressed in the form of $\frac{p}{q}$ where p and q are integers and $q \neq 0$.

Solution: Let $x = 1.272727 \dots$

Since two digits are repeating, multiply by 100

$$100x = 127.2727 \dots$$

$$100x = 126 + 1.272727$$

$$100x = 126 + x$$

$$100x - x = 126$$

$$99x = 126$$

$$x = \frac{126}{99} = \frac{14}{11}$$

$$\therefore 1.\overline{27} = \frac{14}{11}$$

5. Show that $0.2353535\dots = 0.\overline{235}$ can be expressed in the form $\frac{p}{q}$ where p and q

are integers and $q \neq 0$.

Solution: Let $x = 0.\overline{235}$. Here 2 does not repeat, the block 35 repeats. Since 2 digits are repeating we multiply x by 100

$$100x = 23.53535 \dots$$

$$100x = 23.3 + 0.23535 \dots = 23.3 + x$$

$$100x - x = 23.3$$

$$99x = 23.3$$

$$x = \frac{23.3}{99} = \frac{233}{990}$$

Homework:

1. Write the decimal form of the following

(i) $\frac{3}{13}$ (ii) $\frac{1}{11}$ (iii) $\frac{2}{11}$ (iv) $\frac{329}{400}$

2. Express the following in the form of $\frac{p}{q}$, $q \neq 0$

(i) $0.\overline{6}$ (ii) $0.4\overline{7}$

3. Express $0.99999\dots$ in the form of $\frac{p}{q}$